Pair Distribution Computation on GPU

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Goal: Using multidimensional Grid & Block

See B. G. Levine *et al., J. Comput. Phys.* **230**, 3556 (2011) <u>https://aiichironakano.github.io/cs596/Levin-RDFonGPU-JCP11.pdf</u>

cf. https://aiichironakano.github.io/cs596/Grupcev-PairCorr-TKDE13.pdf



• Pair-distance histogram, nhist[Nhbin]

for all histogram bins i
nhist[i] = 0
for all atomic pairs (i,j)

$$++nhist[\lfloor |\vec{r}_{ij}|/\Delta r \rfloor]$$
 count



Pair Distribution Function

• **Pair-distribution function**, g(r) $g(r_i) = \frac{nhist(i)}{2\pi r_i^2 \Delta r \rho N} \xrightarrow{N: \# \text{ of atoms}} \rho: \# \text{ density}$

g(r): For each atom, how many other atoms are distance *r* apart, normalized by # of atoms expected from average density; deviation from 1 signifies correlation with an atom at r = 0

With minimum-image convention,

$$R_{\max} = \sqrt{\sum_{\alpha=x,y,z} \left(\frac{al[\alpha]}{2}\right)^2}$$

$$\Delta r = R_{\text{max}}/N_{\text{hbin}}; r_i = (i+1/2)\Delta r$$

drh





Big Loops over Atomic Pairs

input: r[], n Program: pdf0.c (atomic positions in pos.d)

output: nhis[]

- n: Number of atoms
- r[3*n]: r[3*i|3*i+1|3*i+2] is the xlylz coordinate of the *i*-th atom
- alth[a] = al[a]/2: Half the simulation box lengths

float SignR(float v, float x) {if (x > 0) return v; else return -v;}

Variables in Device Memory



// Compute dev_nhis on GPU: dev_r[] -> dev_nhis[]

cudaMemcpy(nhis,dev_nhis,NHBIN*sizeof(float),cudaMemcpyDeviceToHost);



Who Does What: Nested Decompositions

- Nested block & thread decompositions
 - **>** Spatial decomposition among blocks
 - > Loop-index interleaving among threads within each block

In host program:

dim3 numBlocks(8,8,1);

dim3 threads_per_block(16,16,1);

gpu_histogram_kernel<<<numBlocks,threads_per_block>>>(dev_r,dev_nhis);

in

out



• Use a large enough number of blocks to reduce load imbalance among streaming multiprocessors (SMs)

Device Program for Histogram



Numerical Results



Race Condition

We just "saw" race condition in action!

```
for (int i=iBlockBegin+threadIdx.x; i<iBlockEnd; i+=blockDim.x) {</pre>
  for (int j=jBlockBegin+threadIdx.y; j<jBlockEnd; j+=blockDim.y) {</pre>
    if (i<j) {
      float rij = 0.0;
      for (int a=0; a<3; a++) {
        float dr = r[3*i+a]-r[3*j+a];
        /* Periodic boundary condition */
        dr = dr-d SignR(DALTH[a], dr-DALTH[a])-d SignR(DALTH[a], dr+DALTH[a]);
        rij += dr*dr;
      }
      rij = sqrt(rij); // Pair distance
      int ih = rij/DDRH;
      nhis[ih] += 1.0; // Entry to the histogram
    } // end if i<j
  } // end for j
 // end for i
```

• In newer versions of CUDA, use atomic update atomicAdd(&nhis[ih],1.0);

Compilation on Discovery

• Load the necessary modules

module purge
module load usc/8.3.0
module load cuda

- Compilation of the CUDA program for GPU nvcc -o pdf pdf.cu
- Compilation of the original serial program on CPU for comparison

gcc -o pdf0 pdf0.c -lm

Running CPU & GPU Versions

```
Script: pdf.sl
```

```
#!/bin/bash
#SBATCH --nodes=1
#SBATCH --ntasks-per-node=1
#SBATCH --gres=gpu:1
#SBATCH --time=00:00:59
#SBATCH --output=pdf.out
#SBATCH -A anakano_429
echo '##### CPU: gcc -o pdf0 pdf0.c -lm #####'
./pdf0
echo '##### GPU: nvcc -o pdf pdf.cu #####'
./pdf
```

Output

```
##### CPU: gcc -o pdf0 pdf0.c -lm #####
Execution time (s) = 5.680000e+00
###### GPU: nvcc -o pdf pdf.cu #####
Faster!
Execution time (s) = 6.700000e-01
```

The histogram file, pdf.d, calculated by pdf0 will be overwritten by that by pdf

Numerical Results



Summary: CUDA Pair-Distribution Computing



Finite-Size Effect on g(r)



Geometric Factor in *g*(*r*)



Large-scale Correlation in g(r)



- Short-range correlation (*i.e.* peak positions) unchanged, just magnified by the lower average density, N/V_{expanded}
- Superimposed with larger length-scale geometric factors

Experimental Connection



g(r) of Molten UO₂

• X-ray scattering measurement using synchrotron radiation from 7 GeV electrons at the Advanced Photon Source of the Argonne National Lab.



Neutron Scattering Meets Quantum Neural Network

- Allegro-Legato-PIMD: Incorporate nuclear quantum effect (NQE) through path-integral molecular dynamics (PIMD)
- Neural-network quantum molecular dynamics (NNQMD) trained by quantum molecular dynamics (QMD) achieves long-time Hamiltonian dynamics to resolve fine vibrational structures
- NQE down-shifts inter-molecular vibrational modes in ammonia to explain high-resolution inelastic neutron scattering experiments









\$1.5B Spallation Neutron Source at Oak Ridge National Laboratory

Linker et al., Nature Commun. 15, 3911 ('24)

More Pair-Distribution Computation

<u>Use the force!</u> Reduced variance estimators for densities, radial distribution functions, and local mobilities in molecular simulations **o**



Benjamin Rotenbergª) 匝

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https://aiichironakano.github.io/cs596/Rotenberg-UseTheForce-JCP20.pdf

Extension: Replica Pair Correlation

- Pair correlation beyond Euclidean distance?
- Replica-pair correlation (cosine similarity) to detect replica symmetry breaking (Giorgio Parisi, Nobel physics prize, 2021)

Histogram of correlation between replica pairs (random laser pattern)



• Used to analyze "freezing transitions" of deep neural networks with increasing training data size



H. Yoshino, SciPost Phys. Core 2, 005 ('20)

The Nobel Prize in Physics 2021

The Royal Swedish Academy of Sciences has decided to award the Nobel Prize in Physics 2021

"for groundbreaking contributions to our understanding of complex physical systems"

with one half jointly to

Syukuro Manabe Princeton University, USA

Max Planck Institute for Meteorology, Hamburg, Germany

"for the physical modelling of Earth's climate, quantifying variability and reliably predicting global warming" and the other half to

Giorgio Parisi

Sapienza University of Rome, Italy

"for the discovery of the interplay of disorder and fluctuations in physical systems from atomic to planetary scales"

Replica symmetry breaking