# Molecular Dynamics Simulation: Q&A

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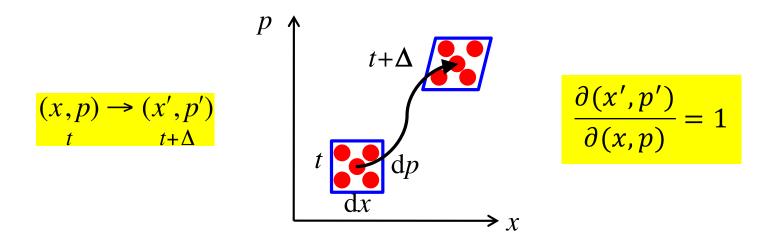
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#### **Liouville's Theorem**

**Q:** Why is it important to preserve the phase-space volume along the molecular-dynamics trajectory?



- A: Exact phase-space-volume conservation tends to provide long-time stability, though formal analysis of long-time accuracy very hard.
- cf. Backward error analysis

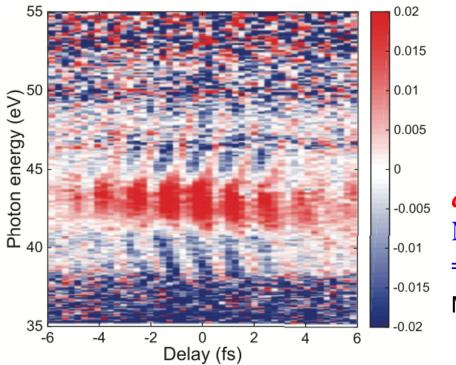
S. Reich, SIAM J. Numer. Anal. 36, 1549 ('99)

### **Velocity Autocorrelation (VAC)**

- **Q: VAC in nonsteady state?**
- **A:** Present it as a function of two time variables.

$$\langle \vec{v}_i(t) \bullet \vec{v}_i(t') \rangle = vac \left( \tau = t - t', T = \frac{t + t'}{2} \right)$$

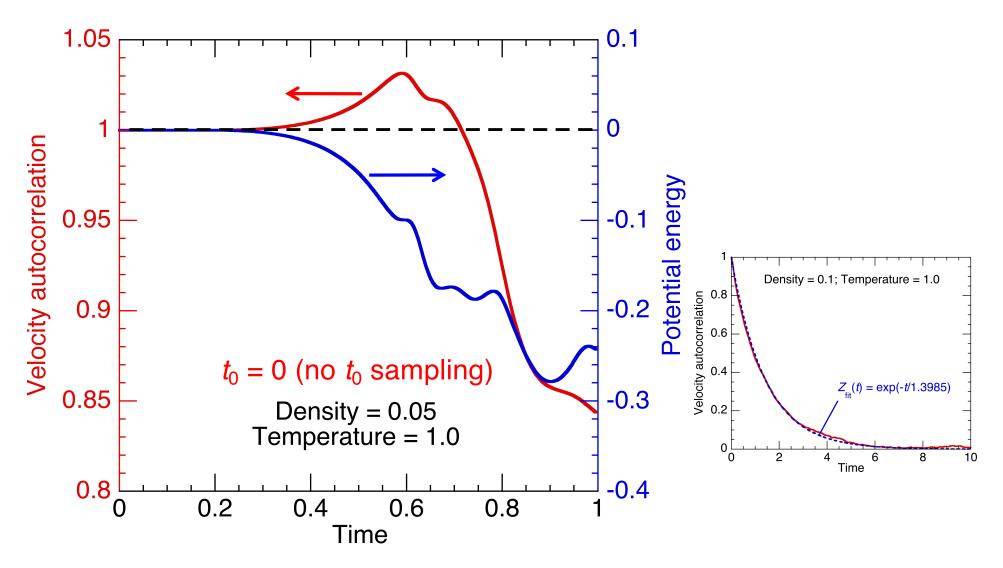
No T dependence in a steady state



# cf. Transient photoabsorption spectrum: Note the atomic-unit energy, 27.2116 eV = h/(0.024 fs); h is Planck's constant M. Lucchini et al., Science 353, 916 ('16)

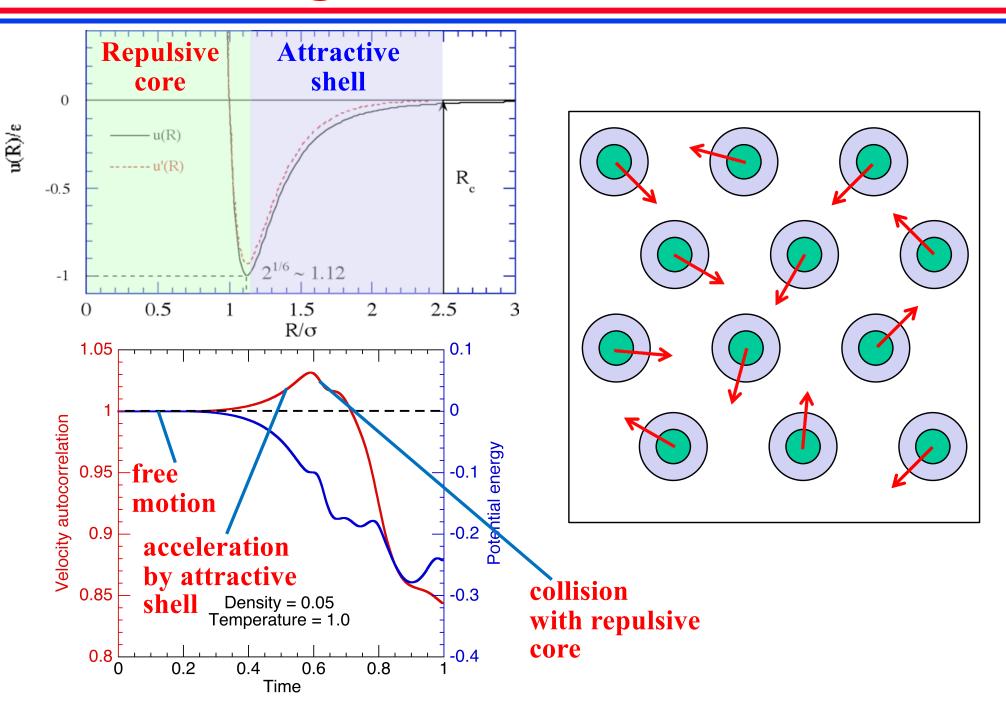
#### **Velocity Autocorrelation > 1?**

• Yes, in a gas phase just when starting from an FCC lattice



• Why? Hint = time variation of the potential energy

#### **Finite-Range Lennard-Jones Potential**



#### **Why Taylor Expansion?**

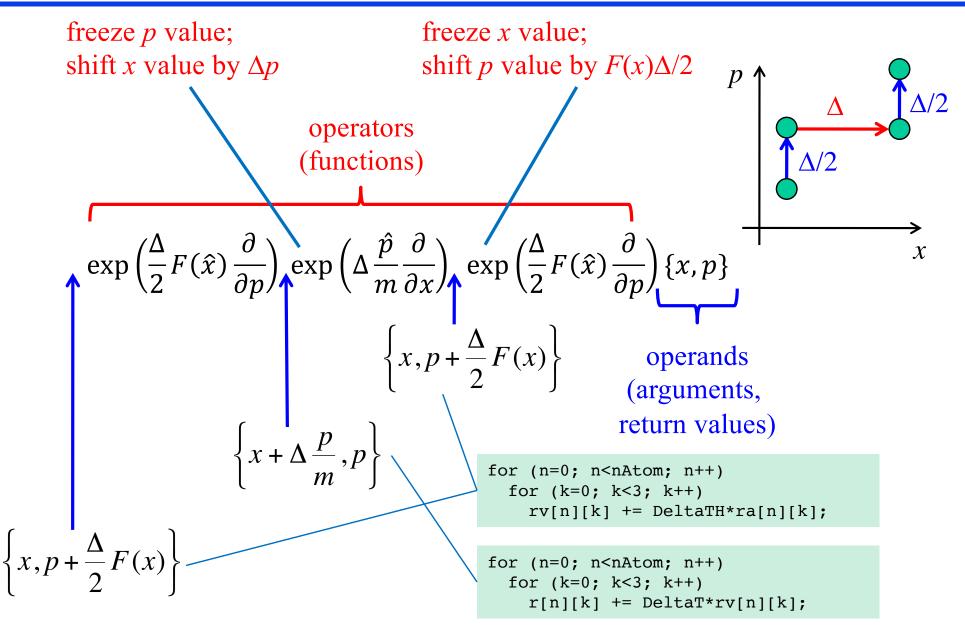
A: Exponentiation of a differential operator is "defined" through Taylor expansion, in which the power of the operator is operationally well defined as successive applications of the operator

$$\left(t\left(F(x)\frac{\partial}{\partial p} + \frac{p}{m}\frac{\partial}{\partial x}\right)\right)^{3}f(x,p) = t\left(F(x)\frac{\partial}{\partial p} + \frac{p}{m}\frac{\partial}{\partial x}\right)\left\{t\left(F(x)\frac{\partial}{\partial p} + \frac{p}{m}\frac{\partial}{\partial x}\right)\left[t\left(F(x)\frac{\partial}{\partial p} + \frac{p}{m}\frac{\partial}{\partial x}\right)f(x,p)\right]\right\}$$

But, it is very hard to obtain a closed form

$$\{?,?\} = \exp\left[t\left(F(x)\frac{\partial}{\partial p} + \frac{p}{m}\frac{\partial}{\partial x}\right)\right] \{x,p\}$$

## **Velocity Verlet Time Propagator?**



**It's shift operation!** 

### **Explicit Form of Mapping?**

